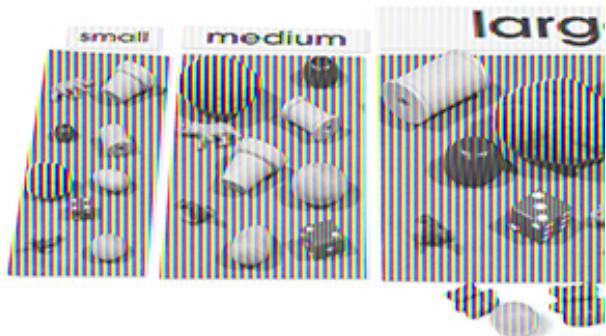


Sorting Videos!

This week is our final topic!

Searching and Sorting Lists of Data



Sort/Search Run-Time

The amount of memory it will take to sort or search an array of n elements. It is denoted as “ $O(n)$ ”, the average sort time.

OK: $O(n^2)$

BEST: $O(n \log n)$

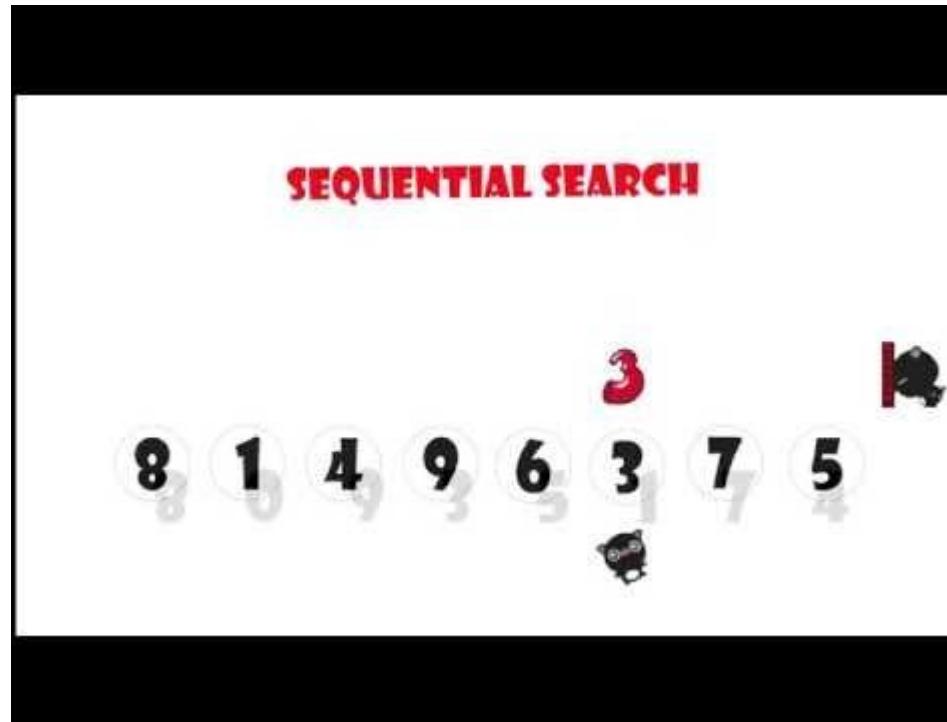
The less efficient but easy to understand sorts

O(n^2):

- Bubble
- Insertion
- Selection

These make **n** passes through an array of length **n** to compare two elements at a time. They have long names which makes it easier to remember they are long sorts.

Linear Search vs Binary Search



Linear Search vs Binary Search

	Linear	Binary
Rules	Can be used on any list	Can only be used on sorted lists
Big-O	n^2	$\log n$

Bubble Sort: run-time $O(n^2)$

- 1) Start at the beginning (or end)**
- 2) The first element looks at the second element. If they are out of order, they switch.**
- 3) The second element looks at the third element. If they are out of order, switch. ETC**
- 4) The biggest element will “float” to the top (or bottom) and be done**
- 5) Start the process over again at the second element.**
- 6) Keep going**

Bubble Sort - Reverse order (Descending)



Selection Sort: run-time $O(n^2)$

- 1) Start at the very beginning of n elements**
- 2) Find the smallest element between 0 and n-1. Put it at index 0.**
- 3) Find the smallest element between 1 and n-1. Put it at index 1.**
- 4) Find the smallest element between 2 and n-1. Put it at index 2.**
- 5) Keep going through n passes**

Selection Sort



Insertion Sort: run-time $O(n^2)$

- 1) Put elements 0 and 1 in the right order
- 2) Take element 2. Put it in the right order with 0 and 1.
- 3) Take element 3. Put it in the right order with 0,1, & 2.
- 4) Keep going through element n-1

Insertion Sort



Warm-Up: AP Sort Question

Given this sorted list; 1, 3, 6, 7, 10, 12, 19

- a) How many comparisons will it take to find the value 10 in a *linear* search?
- b) How many comparisons will it take to find the value 10 in a *binary* search?

Warm-Up: AP Sort Question

Given this sorted list; 1, 3, 6, 7, 10, 12, 19

- a) How many comparisons will it take to find the value 10 in a *linear* search? 5
- b) How many comparisons will it take to find the value 10 in a *binary* search? 3

Warm-Up: AP Sort Question

Given this **unsorted list; 1, 3, 6, 7, 10, 8, 19**

What number will never be found?

Warm-Up: AP Sort Question

Given this **unsorted** list; 1, 3, 6, 7, 10, 8, 19

What number will never be found? **10**

More efficient but harder to understand sorts

$O(n \log n)$: Merge Sort, Quick Sort

These are “DIVIDE AND CONQUER” sorts that RECURSIVELY divide the array into smaller and smaller arrays to be sorted.

Merge Sort



Quick Sort: run-time $O(n \log n)$

- 1) Very similar to merge sort, except the array size is not necessarily *half*. (There are different ways to do this)
- 2) Instead, choose a PIVOT point that divides the array
- 3) Recursively sort the array to the left of the pivot point
- 4) Recursively sort the array to the right of the pivot point
- 5) Keep going until you hit the base cases (you get to a sorted array)
- 6) Merge the sorted arrays

Quick Sort



SEARCH!!!!

Sequential: Start at 0 and check each element until you find the element you need.

Pros: Works on ANY list, easy to code

Con: $O(n)$

Binary: Take a *sorted* list, look in the middle. If the value you want is less, look halfway down. If it's more, look halfway up. Keep halving until you find your value.

‘DIVIDE AND CONQUER’

Pro: Fast! $O(\log n)$

Con: harder to code

Cool Comparison Website

<https://www.toptal.com/developers/sorting-algorithms>

Sequential vs. Binary Search



Binary Search Tree Properties

- The left subtree of a node only contains values that are less than or equal to the node's value.
- The right subtree of a node only contains values that are greater than or equal to the node's value.
- Both left and right subtrees of a node are also binary search trees.



THE MOST
IMPORTANT POINTS
FOR THE AP EXAM...

Linear Search vs Binary Search

	Linear	Binary
Rules	Can be used on any list	Can only be used on sorted lists
Big-O	n^2	$\log n$

Warm-Up: AP Sort Question

Given this sorted list; 1, 3, 6, 7, 10, 12, 19

- a) How many comparisons will it take to find the value 10 in a *linear* search? 5
- b) How many comparisons will it take to find the value 10 in a *binary* search? 3

“DIVIDE AND CONQUER”

- BINARY **SEARCH**
- MERGE & QUICK **SORTS**

(short names, fast search. 5 letters)

Slow Searches - Average efficiency n^2

	Dance	How it works
Bubble	Little Mermaid	<ul style="list-style-type: none">• Items 0 and 1 compare, then swap• Items 1 and 2 compare, then swap..• Items n-1 and n compare then swap• Repeat n times (The biggest item “bubbles” to the top)
Selection	Itik Itik	<ul style="list-style-type: none">• Find smallest item between 0 and n, put at 0• Find the smallest item between 1 and n, put at 1• Find the smallest item between 2 and n, put at 2• Repeat up to finding smallest between n-1, n
Insertion	Navy	<ul style="list-style-type: none">• Put items 0 and 1 in order• INSERT item 2 in the correct spot between 0 and 1• INSERT item 3 in the correct spot between 0 and 2• Keep inserting items into the sorted part of the list• Repeat until you INSERT item n

Fast Searches - Average efficiency $n (\log n)$

DIVIDE AND CONQUER BY USING RECURSION!!

	Dance	How it works
Merge	Buffalo NY, Benny Hill	<ul style="list-style-type: none">• Pick the middle index• Split the list into half at that index• Split each half into half• Keep splitting until you get to the base case of 2 items• Sort the base cases by comparing and swapping• MERGE the lists of length 2• MERGE the lists of length 4• Repeat until you merge $n/2$ and $n/2$
Quick		<ul style="list-style-type: none">• Pick the a “pivot” index that makes sense• Split the list at that index• Split each half into half• Keep splitting until you get to the base case of 2 items• Sort the base cases by comparing and swapping• MERGE the lists of length 2• MERGE the lists of length 4• Repeat until you merge $n/2$ and $n/2$