

# Sorting Videos!

# This week is our final topic!

## Searching and Sorting Lists of Data



## Sort/Search Run-Time

**The amount of memory it will take to sort or search an array of  $n$  elements. It is denoted as “ $O(n)$ ”, the average sort time.**

**OK:  $O(n^2)$**

**BEST:  $O(n \log n)$**

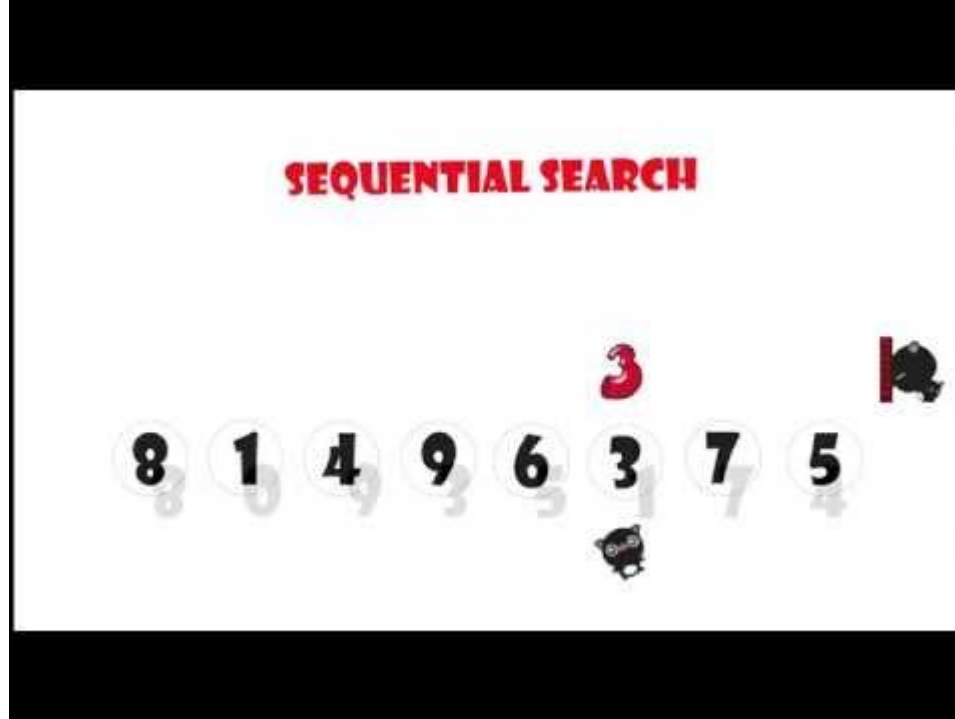
## The less efficient but easy to understand sorts

**$O(n^2)$ :**

- Bubble
- Insertion
- Selection

These make  **$n$**  passes through an array of length  **$n$**  to compare two elements at a time. They have long names which makes it easier to remember they are long sorts.

# Linear Search vs Binary Search



# Linear Search vs Binary Search

	<b>Linear</b>	<b>Binary</b>
Rules	Can be used on any list	Can only be used on sorted lists
Big-O	$n^2$	$\log n$

## **Bubble Sort: run-time $O(n^2)$**

- 1) Start at the beginning (or end)**
- 2) The first element looks at the second element. If they are out of order, they switch.**
- 3) The second element looks at the third element. If they are out of order, switch. ETC**
- 4) The biggest element will “float” to the top (or bottom) and be done**
- 5) Start the process over again at the second element.**
- 6) Keep going**

# Bubble Sort - Reverse order (Descending)





## **Selection Sort: run-time $O(n^2)$**

- 1) Start at the very beginning of n elements**
- 2) Find the smallest element between 0 and n-1. Put it at index 0.**
- 3) Find the smallest element between 1 and n-1. Put it at index 1.**
- 4) Find the smallest element between 2 and n-1. Put it at index 2.**
- 5) Keep going through n passes**

# Selection Sort



## **Insertion Sort: run-time $O(n^2)$**

- 1) Put elements 0 and 1 in the right order**
- 2) Take element 2. Put it in the right order with 0 and 1.**
- 3) Take element 3. Put it in the right order with 0,1, & 2.**
- 4) Keep going through element  $n-1$**

# Insertion Sort



# Warm-Up: AP Sort Question

**Given this sorted list; 1, 3, 6, 7, 10, 12, 19**

- a) How many comparisons will it take to find the value 10 in a *linear* search?**
- b) How many comparisons will it take to find the value 10 in a *binary* search?**

# Warm-Up: AP Sort Question

Given this sorted list; 1, 3, 6, 7, 10, 12, 19

- a) How many comparisons will it take to find the value 10 in a *linear* search? **5**
- b) How many comparisons will it take to find the value 10 in a *binary* search? **3**

# Warm-Up: AP Sort Question

Given this **un**sorted list; 1, 3, 6, 7, 10, 8, 19

What number will never be found?

# Warm-Up: AP Sort Question

Given this **un**sorted list; 1, 3, 6, 7, 10, 8, 19

What number will never be found? **10**



## **More efficient but harder to understand sorts**

**$O(n \log n)$ : Merge Sort, Quick Sort**

**These are “DIVIDE AND CONQUER” sorts that  
RECURSIVELY divide the array into smaller and smaller  
arrays to be sorted.**

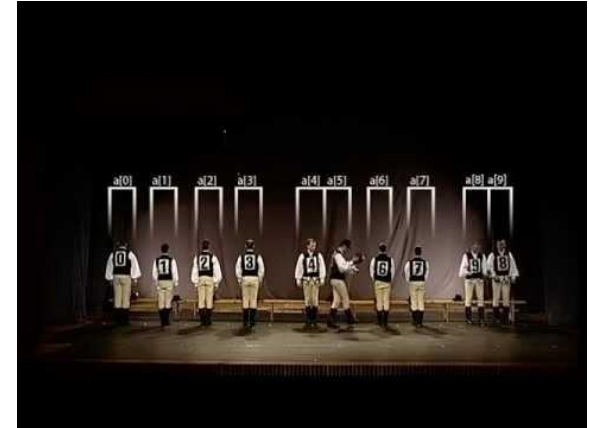
# Merge Sort



## **Quick Sort: run-time $O(n \log n)$**

- 1) Very similar to merge sort, except the array size is not necessarily *half*. (There are different ways to do this)**
- 2) Instead, choose a PIVOT point that divides the array**
- 3) Recursively sort the array to the left of the pivot point**
- 4) Recursively sort the array to the right of the pivot point**
- 5) Keep going until you hit the base cases (you get to a sorted array)**
- 6) Merge the sorted arrays**

# Quick Sort



# SEARCH!!!!

**Sequential**: Start at 0 and check each element until you find the element you need.

Pros: Works on ANY list, easy to code

Con:  $O(n)$

**Binary**: Take a *sorted* list, look in the middle. If the value you want is less, look halfway down. If it's more, look halfway up. Keep halving until you find your value.

**‘DIVIDE AND CONQUER’**

Pro: Fast!  $O(\log n)$

Con: harder to code

# Cool Comparison Website

<https://www.toptal.com/developers/sorting-algorithms>

# Sequential vs. Binary Search

## Binary Search Tree Properties

- The left subtree of a node only contains values that are less than or equal to the node's value.
- The right subtree of a node only contains values that are greater than or equal to the node's value.
- Both left and right subtrees of a node are also binary search trees.



THE MOST  
IMPORTANT POINTS  
FOR THE AP EXAM...



# Linear Search vs Binary Search

	Linear	Binary
Rules	Can be used on any list	Can only be used on sorted lists
Big-O	$n^2$	$\log n$

# Warm-Up: AP Sort Question

Given this sorted list; 1, 3, 6, 7, 10, 12, 19

- a) How many comparisons will it take to find the value 10 in a *linear* search? **5**
- b) How many comparisons will it take to find the value 10 in a *binary* search? **3**

# “DIVIDE AND CONQUER”

- BINARY SEARCH

- MERGE & QUICK SORTS

(short names, fast search. 5 letters)

# Slow Searches - Average efficiency $n^2$

	Dance	How it works
Bubble	Little Mermaid	<ul style="list-style-type: none"><li>• Items 0 and 1 compare, then swap</li><li>• Items 1 and 2 compare, then swap..</li><li>• Items <math>n-1</math> and <math>n</math> compare then swap</li><li>• Repeat <math>n</math> times (The biggest item “bubbles” to the top)</li></ul>
Selection	Itik Itik	<ul style="list-style-type: none"><li>• Find smallest item between 0 and <math>n</math>, put at 0</li><li>• Find the smallest item between 1 and <math>n</math>, put at 1</li><li>• Find the smallest item between 2 and <math>n</math>, put at 2</li><li>• Repeat up to finding smallest between <math>n-1</math>, <math>n</math></li></ul>
Insertion	Navy	<ul style="list-style-type: none"><li>• Put items 0 and 1 in order</li><li>• INSERT item 2 in the correct spot between 0 and 1</li><li>• INSERT item 3 in the correct spot between 0 and 2</li><li>• Keep inserting items into the sorted part of the list</li><li>• Repeat until you INSERT item <math>n</math></li></ul>

# Fast Searches - Average efficiency $n (\log n)$

**DIVIDE AND CONQUER BY USING RECURSION!!**

	Dance	How it works
Merge	Buffalo NY, Benny Hill	<ul style="list-style-type: none"><li>• Pick the middle index</li><li>• Split the list into half at that index</li><li>• Split each half into half</li><li>• Keep splitting until you get to the base case of 2 items</li><li>• Sort the base cases by comparing and swapping</li><li>• MERGE the lists of length 2</li><li>• MERGE the lists of length 4</li><li>• Repeat until you merge <math>n/2</math> and <math>n/2</math></li></ul>
Quick		<ul style="list-style-type: none"><li>• Pick the a “pivot” index that makes sense</li><li>• Split the list at that index</li><li>• Split each half into half</li><li>• Keep splitting until you get to the base case of 2 items</li><li>• Sort the base cases by comparing and swapping</li><li>• MERGE the lists of length 2</li><li>• MERGE the lists of length 4</li><li>• Repeat until you merge <math>n/2</math> and <math>n/2</math></li></ul>